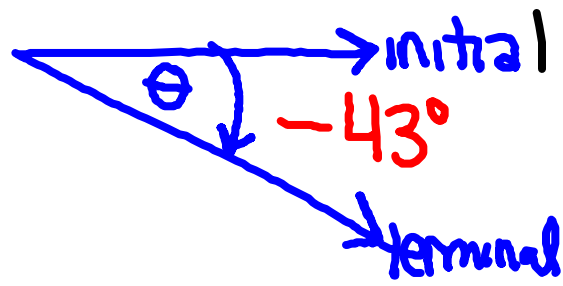
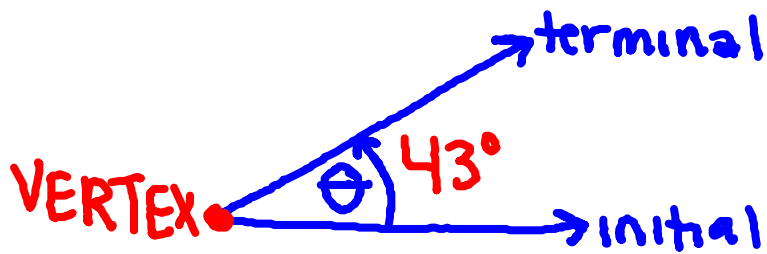


# U2:L1 ANGLES in Standard Position

In trigonometry, angles are made with an initial arm and terminal arm

If the angle of rotation is counterclockwise, then the angle is  $\oplus$

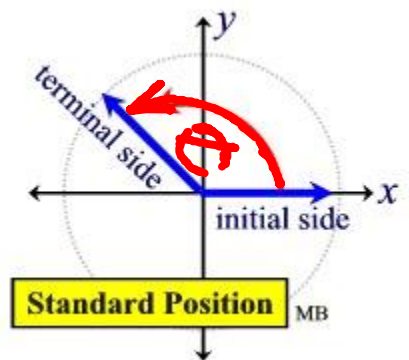
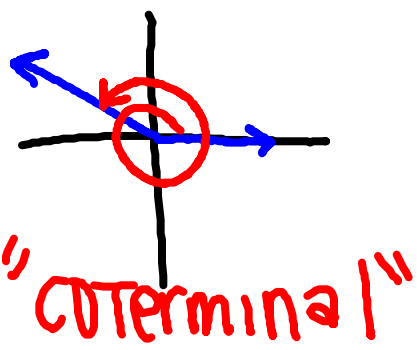


We create angles on Cartesian Planes

The initial arm is always along the x axis and is our starting position.

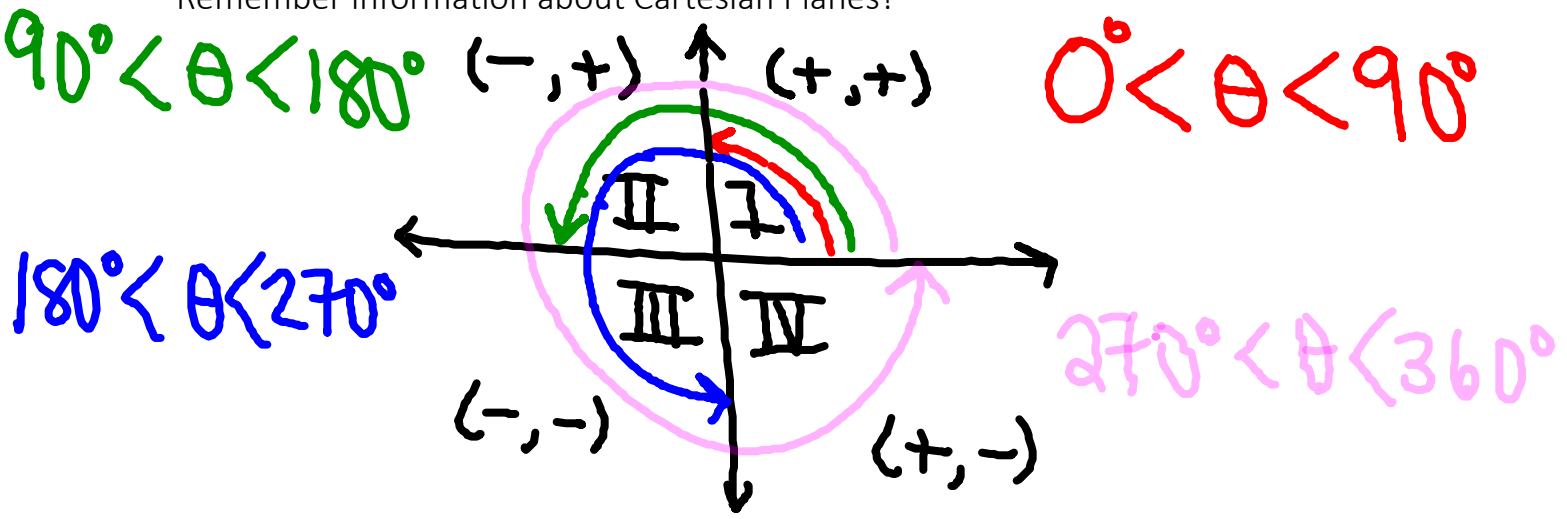
The angle is made at the point of origin (0,0)

The final position, after the rotation about the origin, is the terminal arm



If an angle is set up as such, it is considered an angle in STANDARD POSITION

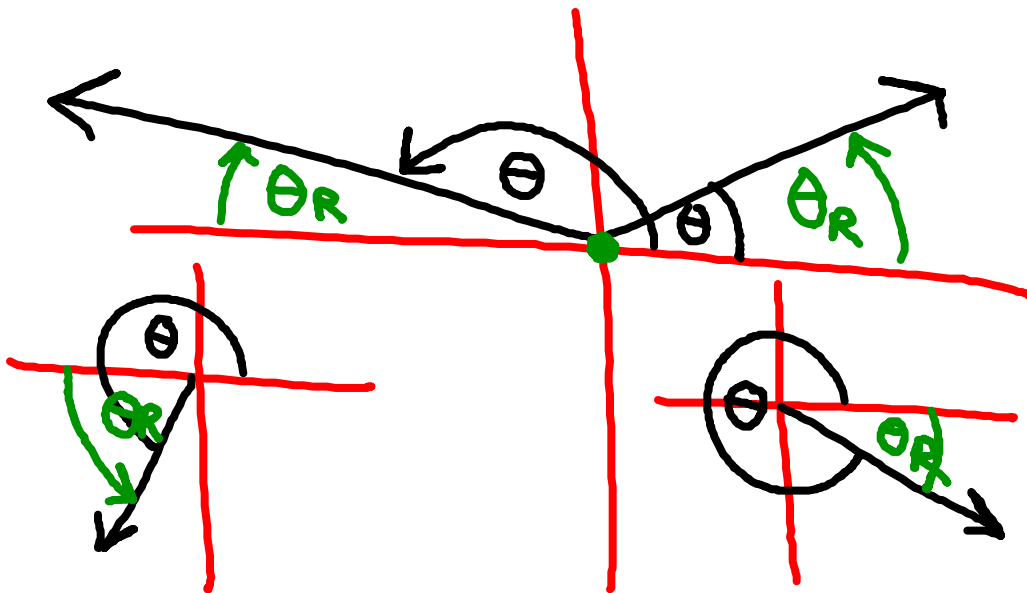
Remember information about Cartesian Planes?



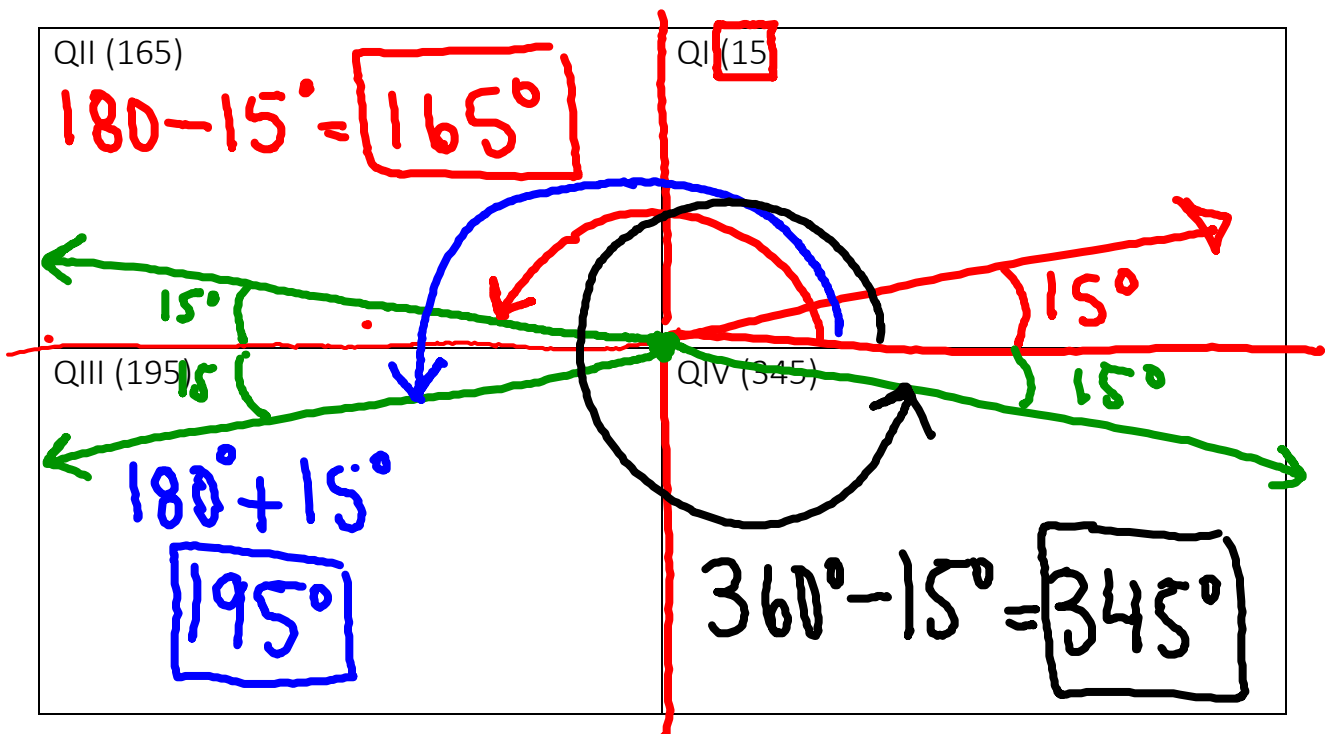
For each angle in standard position, we also have a reference angle

Reference angles ( $\theta_R$ ) are:

- same terminal arm
- vertex @ origin
- initial arm @ x axis



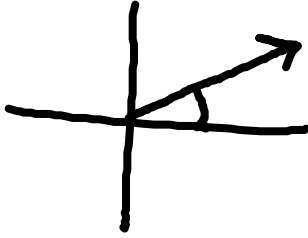
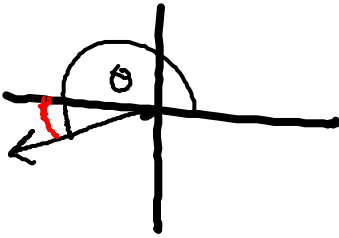
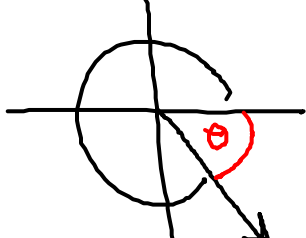
Example: Find the angles which all have a reference angle of  $15^\circ$ .



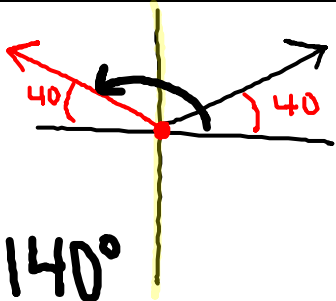
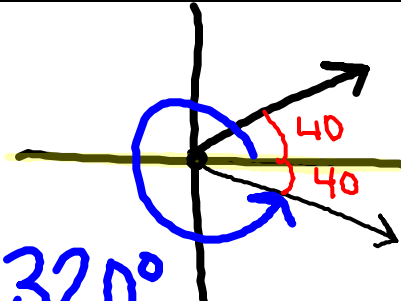
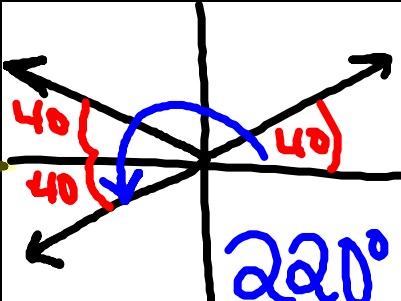
To find the angles, **ADD** or **SUBTRACT** the  $\theta_R$  from  $180^\circ$  and  $360^\circ$  ( $\times$  axis)

Examples:

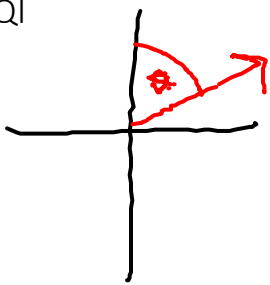
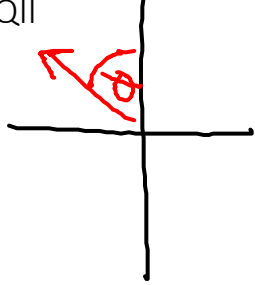
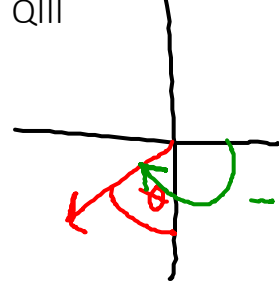
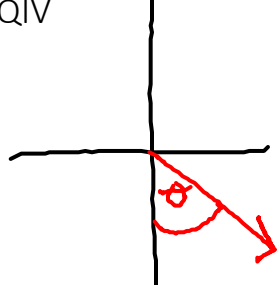
Sketch each angle in standard position. What quadrant are the terminal arms in? What are their reference angles?

$37^\circ$	$207^\circ$	$314^\circ$
		
Q? <b>I</b>	Q? <b>III</b>	Q? <b>IV</b>
$\theta_R?$ <b><math>37^\circ</math></b>	$\theta_R?$ <b><math>27^\circ</math></b>	$\theta_R?$ <b><math>46^\circ</math></b>

Determine the angle in standard position of an angle of  $40^\circ$  when it is:

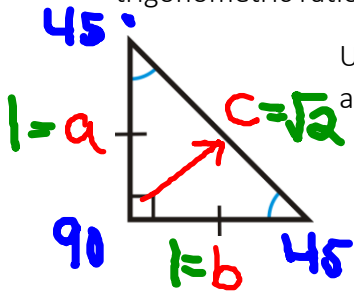
<i>Reflected over the y axis</i>	<i>Reflected over the x axis</i>	<i>Reflected over the y and then x axis.</i>
		
<b><math>140^\circ</math></b>	<b><math>320^\circ</math></b>	<b><math>220^\circ</math></b>

Draw an angle in each quadrant that is not in standard position:

QI	QII	QIII	QIV
			

# SPECIAL RIGHT TRIANGLES

For the angles 30, 45°, 60° you can determine the exact values of their trigonometric ratio.



Using Pythagoras Theorem, we can solve for "c" for this special 45 triangle, with a side length of 1 unit.

$$c^2 = a^2 + b^2$$

$$c^2 = 1^2 + 1^2$$

$$c^2 = 1 + 1$$

$$\sqrt{c^2} = \sqrt{2}$$

$$c = \sqrt{2}$$

SIN	$\frac{O}{H}$	$\frac{1}{\sqrt{2}}$
COS	$\frac{A}{H}$	$\frac{1}{\sqrt{2}}$
TAN	$\frac{O}{A}$	$\frac{1}{1} = 1$

The same can be done with a special 30 triangle, and special 60 triangle.

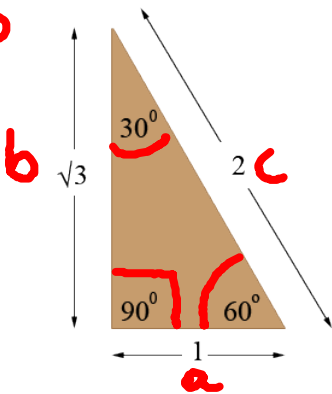
$$c^2 = a^2 + b^2$$

$$c^2 = 1^2 + \sqrt{3}^2$$

$$c^2 = 1 + 3$$

$$\sqrt{c^2} = \sqrt{4}$$

$$c = 2$$



	30°	60°
sin	$\frac{1}{2}$	$\frac{\sqrt{3}}{2}$
cos	$\frac{\sqrt{3}}{2}$	$\frac{1}{2} = \frac{1}{\sqrt{3}}$
tan	$\frac{1}{\sqrt{3}}$	$\frac{\sqrt{3}}{1} = \sqrt{3}$

Ex: A metronome (with an arm of 10 cm) swings from 60° to 120°. What horizontal distance does the tip of the arm move in one beat?



$$\cos = \frac{a}{H}$$

$$\cos 60^\circ = \frac{x}{10}$$

$$\frac{1}{2} = \frac{x}{10}$$

$$x = 5$$

distance  
5 + 5  
**10 cm**

