

U3:L3 Completing the square

Remember, quadratics can be expressed in both...

STANDARD FORM	$f(x) = ax^2 + bx + c$
VERTEX FORM	$f(x) = a(x-p)^2 + q$

Vertex form has advantages because you can identify coordinates of the vertex (p, q) immediately.

The process of converting from standard to vertex form is called completing the square.

The goal of this is to re-write a perfect square trinomial as the square of a binomial.

Remember...

$$a^2 + 2ab + b^2 \quad \leftarrow \text{Perfect Square Trinomial}$$

a^2 \uparrow Square of 1st term a
 $2ab$ \uparrow Twice the product of the two terms
 b^2 \uparrow Square of last term b

$$(a+b)^2 \quad \leftarrow \text{squared binomial}$$

$(x+6)^2$

$$x^2 + 2(x \cdot 6) + 6^2$$

$$x^2 + 12x + 36$$

$$2 \neq 5 \quad (\otimes)$$

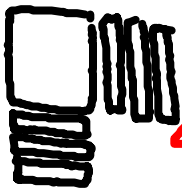
$$2 \neq 5 \quad (\oplus)$$

To help complete the square, we can work with algebra tiles...

$$f(x) = x^2 + 6x + 5$$

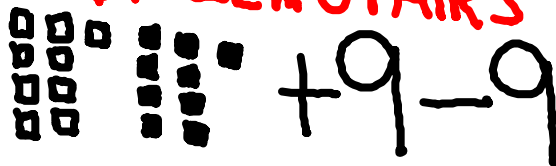


create a square



What do I need?

ADD ZERO PAIRS



$$x^2 + 6x + 9$$

or
 $(x+3)^2$



$$(x+3)^2 - 4$$

leftover

(SF)

(V.F)

(SF)

$$f(x) = 3x^2 - 12x - 9$$



+4

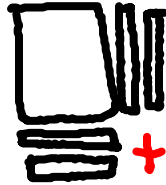
$$x^2 - 4x + 4$$

$$(x-2)^2$$



+4

$$\times 3$$



+4

+12 zero pairs
~~-12~~

leftover

$$-12 + (-9)$$

$$-21$$

(VF) $3(x-2)^2 - 21$

$$f(x) = -5x^2 - 70x$$

Some equations are too big to solve with tiles... therefore we need to solve algebraically...

|| No drawing

Algebraically...

$$f(x) = x^2 + 6x + 5$$

$$y = x^2 + 6x + 5$$

$$y = (x^2 + 6x) + 5$$

$$y = (x^2 + 6x + 9 - 9) + 5$$

$$y = (x^2 + 6x + 9) - 9 + 5$$

$$y = (x+3)^2 - 9 + 5$$

$$y = (x+3)^2 - 4$$

* group 1st 2 terms

* + and - square of $\frac{1}{2}b$

$$6 \div 2 = 3^2 = 9$$

* group perfect square trinomial

* Find square binomial

* Simplify

$$f(x) = 3x^2 - 12x - 9$$

$$y = (3x^2 - 12x) - 9$$

$$y = 3(x^2 - 4x) - 9$$

$$y = 3(x^2 - 4x + 4 - 4) - 9$$

$$y = 3(x^2 - 4x + 4) - 12 - 9$$

$$y = 3(x-2)^2 - 21$$

$$\frac{-4}{2} = -2^2 = 4$$

$$f(x) = -5x^2 - 70x$$

Verifying Equivalency

Convert $y = 4x^2 - 28x - 23$ to vertex:

Verify:

Work Backwards

